

P11. Given Taylor series, a value of sine function can be approximated from

$$\sin(x) \approx \sum_{n=0}^{M-1} \frac{(-1)^n}{(2n+1)!} \cdot x^{2n+1},$$

where M is a number of terms. The larger M is, the more accurate the approximate is. For example,

$$M=5, \sin(x) \simeq x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \frac{x^9}{9!}.$$

$$M=6, \sin(x) \simeq x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \frac{x^9}{9!} + \frac{x^{11}}{11!}.$$

Write a program to approximate a sine value: ask a user for x for an angle in radian and M for a number of terms, compute a value of $\sin(x)$ for M terms, and report the computation.

Use the P11 template. (P11_template.py. The template is only to ensure the exact display format and allows smooth auto-grading.)

Example:

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x:0.7

M:2

$\sin(0.70) = 0.64283$

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x:0.7

M:3

$\sin(0.70) = 0.64423$

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x:0.7

M:4

$\sin(0.70) = 0.64422$

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x:0.7

M:5

$\sin(0.70) = 0.64422$

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Here is P11_template.py

```
"""
Given Taylor series, a value of sine function can be approximated from
 $\sin(x) \approx \sum_{n=0}^{M-1} \frac{(-1)^n}{(2n+1)!} x^{(2n+1)}$ ,
where M is a number of terms. The larger M is,
the more accurate the approximate is. For example,
M = 5,  $\sin(x) \approx x - x^3/3! + x^5/5! - x^7/7! + x^9/9!$ .
M = 6,  $\sin(x) \approx x - x^3/3! + x^5/5! - x^7/7! + x^9/9! + x^{11}/11!$ .
Write a function, named approx_sin(x, tol),
to take 2 argument: x for an angle in radian and tol for tolerance.
The function computer approximate value of sin(x) for M terms such that
the last term in the series is smaller than the tolerance.
"""

def fact(n):
    f = 1
    for i in range(1,n+1):
        f *= i

    return f

def approx_sin(x, M):
    sinv = 0

    # Write your code here!!!

    return sinv

if __name__ == '__main__':
    x = float(input('x:'))
    M = int(input('M:'))

    print('sin(%.2f) = %.5f'%(x, approx_sin(x, M)))
```